Mth 111 Final Exam

You must show the solution process not merely the answer to receive full credit. Write in a neat and organized fashion. *Circle or box-in* your answers. 100 pts.

Name

Solving Equations You must show the solution process not merely the answer. Check your Answers!

Franz Helfenstein

1)	Solve for x:	$2 - 3 \cdot \frac{5 - 3x}{4} = \frac{3x}{5}$	5 pts
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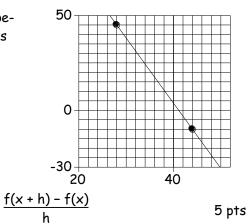
2) Solve for x: (x - 5)(x + 4) = 2(x - 5) + 18

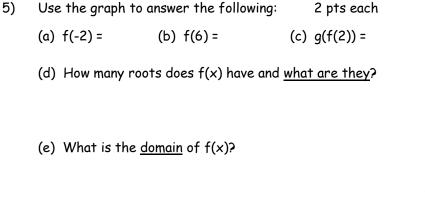


5 pts

 Use the indicated points to find the equation of this line in slopeintercept form. Show your work for full credit.

4) For $f(x) = 1 + x^2$ compute and simplify the difference quotient. $\frac{f(x + x)}{x}$





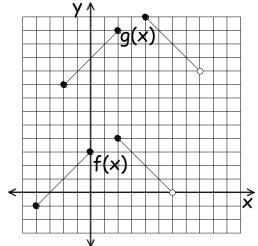
- (f) Give all x-values for which f(x) = 3. x =
- (g) Circle the correct version of g(x) as a translated version of f(x).

g(x) = f(x + 2) + 9 g(x) = f(x - 2) + 9 g(x) = f(2x + 2) + 9 g(x) = f(4) + 9

6) Find the <u>average rate of change</u> from $x_1 = 1$ to $x_2 = 4$ for the function $y = \frac{x^2 - 4}{2}$ 5 pts

7)
$$f(x) = \frac{4-5x}{3}$$
. Find $f^{-1}(x)$. 5 pts

- 8) Use the polynomial, $P(x) = 7x^2(x + 5)(x 4)^3$ to answer the following. 4 pts (a) What is the order of P(x)? _____ (b) What are the roots for P(x)? _____
- 9) An alien object is growing exponentially. When first discovered, it had a mass of 200# but now, 7 days later, it has a mass of 2500#. What is its exponential growth rate? Use P = P₀e^{rt}.



10) Give the domain of each of these functions:

(a)
$$y = \frac{e^x}{(x-1)(x+1)}$$
 (b) $y = \frac{\ln(x-1)}{x}$

- 11) 2 pts ea
- a) Combine factors and convert
 b) Simplify to a single term
 c) Simplify to a single integer.
 to all positive exponents
 ln 2x² 2ln x =
 log₂ 100 log₂ 25 =

$$\frac{(x^3 \gamma)^3 x^{-8}}{x^4 y^5} =$$

12) $f(x) = 3x^2 - 1$ $g(x) = \sqrt{2x - 1}$ Simplify the following: 3 pts each (a) $[g(x)]^{-1} =$

(b) f(g(2)) =

(c) $g^{2}(x) =$

- 13) $H(x) = 8xe^{-x/25}$ represents hay production in a field. Hay Volume x = 0 corresponds to beginning of irrigation. 2 pts each 50 (a) Draw the graph of H(x). (b) How many days after start of irrigation should the farmer harvest to obtain the maximum amount of hay? 0-50 100 0 (c) The farmer stops irrigating when H(x) drops to 10. How days many days is that? Round your answer to the nearest day.
- 14) Using the <u>TI graphing features</u>, solve $e^{0.2x} = 12 + 5x$. Give answer to nearest <u>hundredth</u> 2 pts

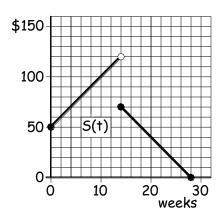
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2 pts ea

15) Write S(t) as a piecewise function. Include domains. 4 pts

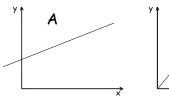
$$S(t) = \begin{cases} \\ \\ \\ \end{cases}$$

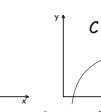
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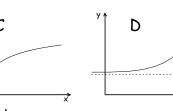


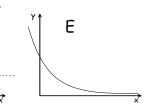
16) From this list, choose the letter that most closely associates with the graphs shown. Then write that letter on the graph. Not every letter will be used. Assume a, b, c > 0 5 pts

(A) piecewise fcn	(B) quadratic fcn	(C) cubic fcn	(D) $\gamma = \frac{a}{x - b}$	(E) y = ln (ax + b)
(F) y = (x - a) ⁵	(G) y = ae ^{-x} + c	(H) ax - by + c = 0	(I) y = a e ^{-bx}	(J) $y = a(e^{bx}) + c$









17) Solve the following equations for y 3 pts each

В

(a) $x = 4 + e^{-2\gamma}$

(b)
$$x = \ln(3y) + 5$$

BONUS

The following data represents mercury concentration found in the sediment at the bottom of Lake Superior.

Sediment Depth (cm)	20	40	60	80
Concentration (ppb)	42	62	58	29

- (a) Using the <u>appropriate regression</u> equation, what is the predicted worst pollution concentration and at what depth is it expected to be found?
- (b) Using your regression equation, at what depth is contamination expected to be zero?