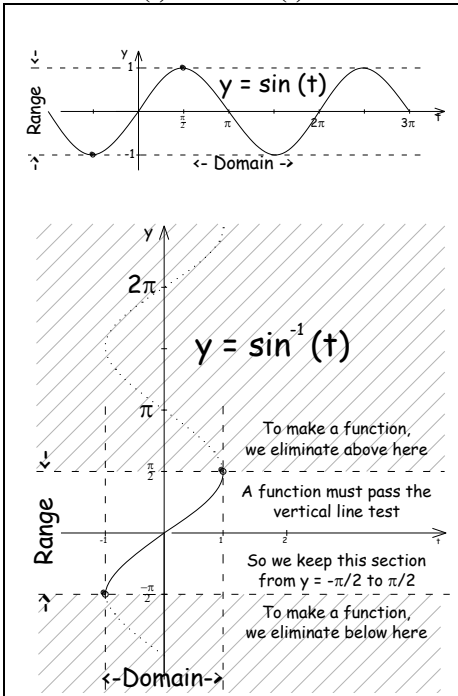


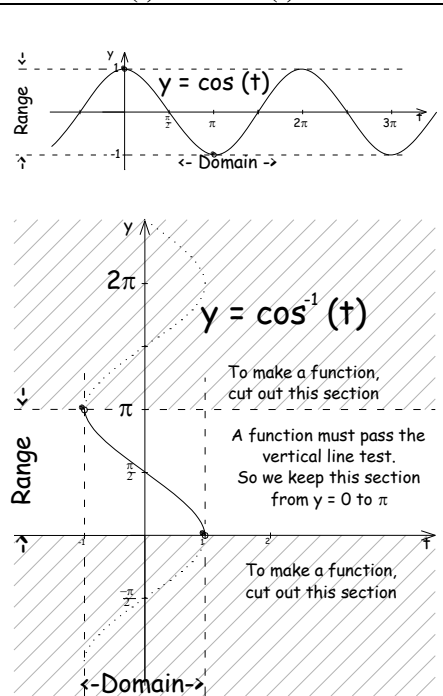
# TRIGONOMETRIC FUNCTIONS

Note: All these formats are interchangeable:  $\sin^{-1} t = \text{invsin } t = \text{arcsin } t$

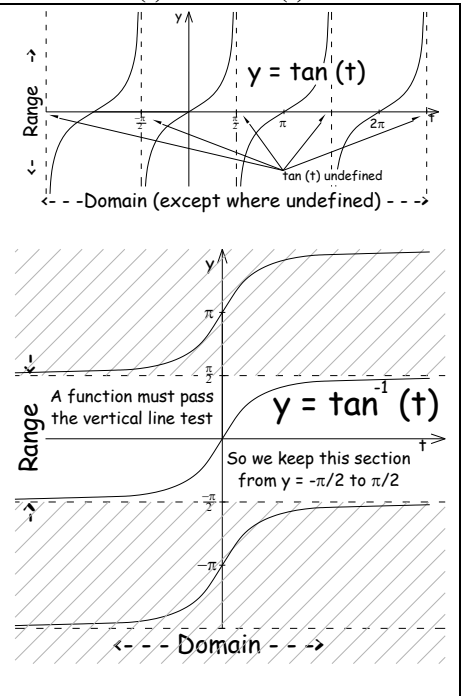
## The sin (t) and sin<sup>-1</sup> (t) functions



## The cos (t) and cos<sup>-1</sup> (t) functions



## The tan (t) and tan<sup>-1</sup> (t) functions



| Table of Domain and Range for Basic Trig functions. | Function | $y = \sin t$        | $y = \cos t$        | $y = \tan t$                | $\sin \theta$     | $\cos \theta$ | $\tan \theta$       |
|---|----------|---------------------|---------------------|-----------------------------|-------------------|---------------|---------------------|
|   | Domain   | $(-\infty, \infty)$ | $(-\infty, \infty)$ | $t \neq \pm\pi/2 \pm 2n\pi$ | $[-1, 1]$         | $[-1, 1]$     | $(-\infty, \infty)$ |
|   | Range    | $[-1, 1]$           | $[-1, 1]$           | $(-\infty, \infty)$         | $[-\pi/2, \pi/2]$ | $[0, \pi]$    | $(-\pi/2, \pi/2)$   |

For Geometric uses of trigonometric functions

|  |  |  |   |   |  |
|--|--|--|---|---|--|
| y is a ratio of sides<br>y is non-dimensional<br>i.e. y is always unitless | $y = \sin t$<br>$y = \cos t$<br>$y = \tan t$ | t is an "angle"<br>t is in either deg or radians | y is an "angle"<br>y is either deg or radians | $y = \sin^{-1} t$<br>$y = \cos^{-1} t$<br>$y = \tan^{-1} t$ | y is non-dimensional<br>i.e. y is unitless |
|--|--|--|---|---|--|

## GRAPHING BASICS

Notation for  $y = A \sin[b(t - h)] + k$

One Period (p) = One Wavelength (λ) = Time of One Cycle (T)

Frequency (f) = cycles/sec = Hertz (Hz).  $f = 1/T = b/(2\pi)$

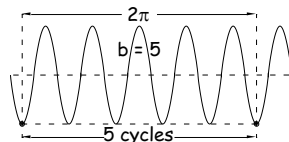
A = amplitude. Max/min displacement from equilibrium

h = horizontal shift ('-' shift right), k = vertical shift ('+' shift up)

b = the number of cycles in  $2\pi$ .

Sometimes you can easily count 'b'.

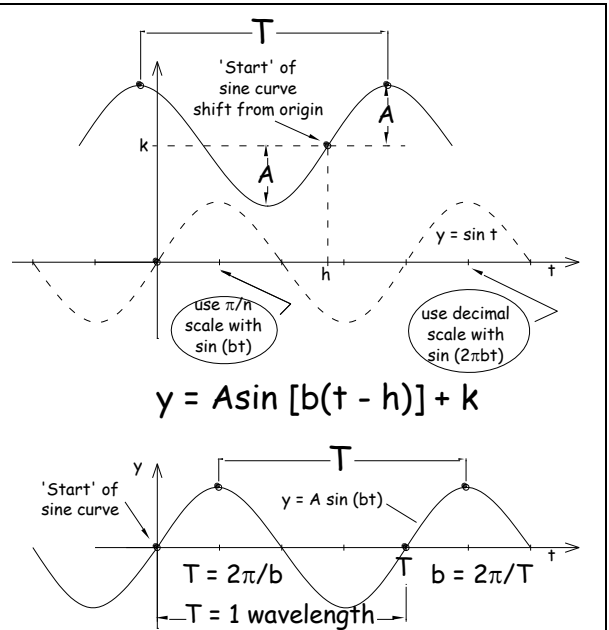
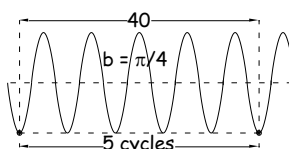
In this example, b = 5.



Sometimes you must compute b.

To compute b, measure one or more waves to compute T. Then  $b = 2\pi/T$ .

Here  $T = 40/5 = 8$ .  $b = 2\pi/8 = \pi/4$



Here  $T = 40/5 = 8$ .  $b = 2\pi/8 = \pi/4$

For  $y = f(x) \sin (bx)$ ,  $f(x)$  acts as the amplitude for  $\sin (bx)$

Here,  $f(x)$  is a linear function of the form  $mx$ . To find  $m$ , use any local max data point.

